

GOSHEN COLLEGE MATHEMATICS DEPARTMENT MATH 323 PROBABILITY & STATISTICS – SPRING 2021-21

Catalog Description

(3 credits) An introduction to the theory, practice and computer simulation of probability and statistics. Data exploration, sample spaces, random variables, probability distributions and their derivations, probability simulations and statistical inference. Prerequisite: Math 211 and either Math 205 or 212.

Content

Observations, experiments, and simulations generate data. This course studies techniques for summarizing data with graphs and numbers and how data can be used to infer something about the phenomena from which the data were generated. These techniques depend upon an understanding of the probability of events arising from idealized populations. There will be a balance between how to use the techniques and the theoretical underpinnings of the techniques.

Learning Objectives

The student will be able to do the following:

- 1. Identify and distinguish between population and sample, parameter and statistic, theoretical and empirical, quantitative and qualitative, variable and data, experiment and observation, random and convenience sample, random variable and sample space.
- 2. Estimate, compute, and interpret descriptive statistics (e.g., mean, median, standard deviation, percentiles, correlation, best-fit linear model parameters).
- 3. Construct and interpret graphical summaries of data (e.g., histogram, box plot, scatter plot, quantile-quantile plot).
- 4. Use software for statistical computation and simulation.
- 5. Describe and identify theoretical, empirical, and subjective forms of probability.
- 6. Define and identity independent events and random variables.
- 7. Compute unconditional and conditional probabilities using systematic enumeration, addition and multiplication rules, complements, permutations, combinations, Bayes' Theorem, and simulation.
- 8. Use probability distributions (e.g., uniform, binomial and Poisson) and densities (e.g., uniform, normal, and gamma) to compute probabilities and expected values.
- 9. Compute (via normal and simulation approximation) and interpret confidence intervals for simple parameters (e.g., mean and standard deviation).
- 10. Compute and interpret simple hypotheses tests (e.g., mean, difference in means, and model fit).
- 11. Derive formulas for use in linear best fit, probability distributions, random variable distributions, parametric confidence intervals, test statistic distributions.
- 12. Learn mathematics by reading, listening, exploring, and conversing in an effective manner.
- 13. Explain mathematical reasoning through writing in a precise and articulate manner in both informal and formal settings.
- 14. Exhibit curiosity, playfulness, creativity, confidence, perseverance, interest in multiple perspectives, and a collaborative spirit.

Activities

The study of mathematics is not a spectator sport! Reading, listening, solving problems, writing explanations, reflecting upon ideas, and receiving feedback are essential to learning mathematics. Read with paper and pencil in hand, and take an anticipatory approach: try to obtain solutions, explanations, and proofs before reading what the author provides. Write down specific questions when you do not understand a portion of the text or a lecture. Try to recreate the key ideas, solve problems, and write proofs without looking at the book or notes.

An average student can obtain an average grade with an average of nine hours each week devoted to this course—adjust if you are not average or desire a grade that is not average.

Instructor David Housman, SC 117, dhousman@goshen.edu, 535-7405.

See office door or Moodle for availability.

Class Time MWF 3:00 - 3:50pm in SC 006.

Textbook There is no required text for this course; however, I will often refer to Johannes Ledolter and Robert V.

> Hogg, Applied Statistics for Engineers and Physical Scientists, 3rd edition, Pearson Education, 2010, ISBN: 978-0-13-601798-1. A copy of this book and the student solutions manual will be available on

the Good Library reserve shelf.

On-line Moodle https://moodle.goshen.edu contains all course information. Announcements posted to the forum

will be emailed to all students.

Software The statistical programming language R and the integrated development environment RStudio will be used. Both are freely available open-source software and are installed on campus lab computers. We

may also use the statistical software program Minitab, which is installed on campus lab computers and is available for rent at a reasonable price. Sage (sagemath.org) and its collaborative notebook interface

CoCalc (cocalc.com) may also be used for symbolic computation.

Notebook A three-ring binder with loose-leaf lined and graph paper is recommended so that you can keep a written

record of problem-solving attempts, questions, math discoveries, and skill assessments.

Grades will depend upon your performance on assignments (60%), one midterm exam (20%), and a final

exam (20%). If beneficial, your final exam grade will replace your grade on the midterm exam. In order to receive a passing grade in this course, the average of your exam scores or your final exam score must be 60% or higher—regardless of your non-exam scores. A semester average of at least 90%, 80%, 70%, and 60% will earn a grade of A-, B-, C-, and D, respectively. Some upward adjustment may be made

based upon class participation and individual effort and progress.

Assignments Achieve and demonstrate understanding by completing the assigned exercises. Your solutions will be evaluated on the correctness of your mathematical descriptions and arguments, the clarity of your

writing, and the quality of your presentation.

Assignments are typically due at the *start* of or *before* the class after the class during which the corresponding topic was discussed. Individual exercise solutions can be resubmitted or submitted late by the class period after the first submissions are graded and returned to students, but a 30% penalty will be assessed on these resubmissions and late submissions. When resubmitting work, include the originally

graded work.

Grading

Extra Credit

You are encouraged to collaborate and seek assistance when having difficulties. You will have achieved the expected level of understanding when you are able to obtain your own solutions, independently

reproduce solutions developed in collaboration or with assistance, and/or explain a solution to others.

errors in the text or posted course materials and describe the error; (2) attend a quantitative presentation (e.g., Science Speakers) or participate in a quantitatively based activity and describe in writing some interesting mathematical aspect of the presentation or activity; or (3) participate in a <u>Career Networks</u> event and describe your most important discovery. Turn in to the instructor a single piece of paper

Receive extra credit toward your assignments grade by doing one or more of the following: (1) find

containing your description.

Exams Exhibit your mastery of the learning objectives without assistance or collaboration. There may be both

in-class and take-home portions for each exam.

Tutoring The Academic Success Center provides limited tutoring and writing support for free to all undergraduate students. Make an appointment at goshen.edu/asc. However, it is unlikely that the ASC can hire

someone with adequate knowledge of this course. Your best option is to ask the instructor!

Disability Services

Goshen College is committed to providing all students equal access to programs and facilities. Students who need accommodations based on disability should contact the Director of the Academic Success Center (ASC). Students must register with ASC before faculty are required to provide reasonable accommodations. For more information or to register, please contact the Director of the ASC, Judy Weaver, Good Library 112, jweaver@goshen.edu or 574-535-7560. To ensure that learning needs are met, contact the director of the ASC the first week of classes.

Collaboration and Academic Integrity

You are encouraged to use all available resources in order to learn the concepts and techniques discussed in this course. In particular, conversations with other students and the instructor can be an effective learning method. Reading other books and web pages can be another effective learning method. However, copying someone else's work subverts the learning process.

For assignments, you may look at and discuss another student's work, but any written work developed during collaboration with another student should be destroyed before writing your own solutions. You should give written acknowledgement to people with whom you have had discussions and to any written materials (other than the text) that were helpful.

For exams, you may *not* use any resources unless a specific exception is stated by the instructor.

Failure to observe the above rules will result in a zero on the assignment or exam. Any violation of academic integrity will be reported to the Academic Dean. Observation of the above rules will help you learn the material well and give you the satisfaction of knowing that you have earned your grade.

Due Date Policy

Class participation, assignments, labs, and exams can only be excused, rescheduled, or made up if (1) there is a serious medical problem, a death in the immediate family, or an irreconcilable conflict with another official Goshen College activity; (2) there is written documentation signed by proper authorities; and (3) the instructor is notified prior to the due date or as soon as possible afterwards.